

# N-body/SPH and galaxy evolution

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N-body/SPH  
and galaxy  
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# N-Body

The concept behind N-Body simulations

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## Simulations of dynamical system of particles

- ▶ Particles are under the influence of physical forces such as gravity
- ▶ Force exerted on each particle arises from its interaction with all the other particles

Two parts are essential to any N-Body code:

- ▶ The **force calculator routine**, which computes forces
- ▶ The **integrator**, which integrates the equations of motion

# Force routine methods

## Overview of force calculator methods

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Compute forces from physical quantities (mass, charge, etc.)

- ▶ PP (Particle-Particle)
- ▶ PM (Particle-Mesh)
- ▶ Tree
- ▶ P<sup>3</sup>M (Particle-Particle/Particle-Mesh)
- ▶ Fourier

# Particle-Particle

## Force routine methods

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The force acting on particle  $i$  is computed using all the other particles.

$$\vec{F}_i = m_i \vec{a}_i = - \sum_{j \neq i} \frac{G m_i m_j}{r_{ij}^3} \vec{r}_{ij}$$

- ▶ Very straightforward
- ▶ Computationally inefficient  $\sim O(n^2)$
- ▶ Unappropriate to simulate large systems
- ▶ Cool enough for clusters and simulations of close-range dynamics

# Particle-Mesh

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Space is divided up with a mesh of density values

- ▶ Particles no longer interact with other particles
- ▶ Potential energy of each point in the mesh calculated through FFT (Fast Fourier Transform) techniques

$$\nabla^2\Phi = 4\pi G\rho$$

- ▶ Forces applied to particles based on the cell they're in
- ▶ More efficient than PP, usually  $\sim O(n+n_g \log(n_g))$
- ▶ Does not handle particle interactions
- ▶ Thus, it is obsolete to P<sup>3</sup>M

# Tree codes

## Force routine methods

### Force superposition concept

- ▶  $F = F_{external} + F_{nearest\_neighbours} + F_{far\_field}$
- ▶ QuadTree in 2D, OctalTree in 3D
- ▶ Each node contains mass and position of subsquare CM
- ▶  $\sim O(n \log(n))$

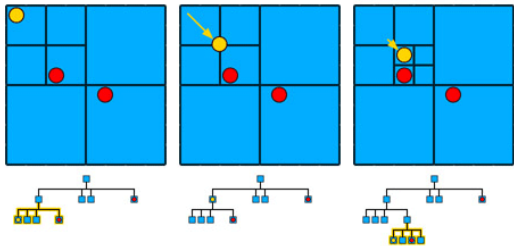


Figure: Quadtree evolution with time



# Integrator methods

## Overview of integrator methods

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Various methods for integrating differential equations from forces to find out  $x_j$ ,  $\dot{x}_j$ ,  $\ddot{x}_j$

- ▶ **Euler**, 1st order - Calculate all values at each time step
- ▶ **Leapfrog**, 2d order - Calculate velocities and positions interleaved in time
- ▶ **Runge-Kutta methods**
- ▶ **Symplectic integrators**, based on canonical transformations

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SPH is a computational method used to simulate fluid flows.

- ▶ Fluid is divided into a set of discrete elements, referred to as particles, from which continuous properties are derived
- ▶ Particles have a *smoothing length*,  $h$ , over which physical properties are smoothed by a kernel function,  $W$
- ▶ Contribution of particle to a property weighted according to distance and density

$$F(r_i) = \sum_{j=1}^n F_j \frac{m_j}{\rho_j} W(|r_{ij}|, h_j)$$

$W$ : Gaussian function, cubic spline, etc.

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## GADGET-2

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The starting point is the GADGET-2 code for cosmological N-body/SPH simulations

- ▶ Collisionless fluid (stars, DM) computed with a **TreePM** n-body algorithm
  - ▶ **Tree** scheme used for short-range forces
  - ▶ **FFT-based PM** scheme used for long-range forces
- ▶ The collisional component (gas) is described using SPH

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# Modelling the galaxy evolution

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## Galactic evolution ingredients to add to our barebones code

- ▶ Radiative cooling
- ▶ Star formation
- ▶ Gas restitution
- ▶ Supernova energy feedback
- ▶ Chemical enrichment
- ▶ White Dwarf population
- ▶ AGN outflow

# Radiative Cooling

Mechanism responsible (among others) for galaxy and star formation: collapse through internal energy decrease

- ▶ Variation of  $u$  due to expansions and contractions of gas and viscosity process (already in GADGET-2)
- ▶ Decrease of  $u$  due to radiative non conservative process of cooling

$$\begin{aligned}\left(\frac{du}{dt}\right) &= \left(\frac{du}{dt}\right)_{vis} + \left(\frac{du}{dt}\right)_{rad} \\ \left(\frac{du}{dt}\right)_{vis} &= -\frac{P}{\rho} \nabla \cdot \mathbf{v} \\ \left(\frac{du}{dt}\right)_{rad} &= -\frac{\Lambda(u, \rho)}{\rho}\end{aligned}$$



# Star formation (1/2)

## Step 1 - Election of candidate particles

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SF → convert gas particle to stellar particle. Conditions:

1. Gas particle must be shrinking

$$\nabla \cdot \mathbf{v}_i < 0$$

2. Jeans criterion must be met locally: Gravity force larger than force due to pressure gradient

$$\frac{h_i}{c_i} > 1 / \sqrt{4\pi G \rho_i}$$

3. When collapsing, the gas particle must not gain heat

# Star formation (2/2)

## Step 2 - Convert fluid element into stars

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Particle  $i$  eligible to star formation if it satisfies conditions. Then, convert selected fluid particles into stars according to SF rate

$$\frac{d\rho_*}{dt} = -\frac{d\rho_g}{dt} = c_* \frac{\rho_g}{\tau_{ff}}$$

$$f = P(SF) = 1 - \exp\left(-c_* \frac{\Delta t}{\tau_{ff}}\right)$$

# Gas restitution

How to model the return of enriched material from evolved stars to ISM

- ▶  $P[\text{gas} \rightarrow \text{star}] = \text{SFR}$ ,  $P[\text{star} \rightarrow \text{gas}] = ?$
- ▶ Stochastic algorithm, no instantaneous recycling of material
- ▶ Baryonic particle: Gas, Star, Remnant
- ▶ Considering  $T = T_H - t_0$ ,

$$1 = \int_{m(T)}^{m_{\max}} \Phi(m) dm + \int_{m_{\min}}^{m(T)} \Phi(m) dm$$

- ▶ Divide SSP in  $E_{SSP}(T)$ ,  $R_{SSP}(T)$  and  $LM_{SSP}(T)$ . Draw  $R_{\text{and}} \text{in}[0, 1]$

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# Supernova energy feedback

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Energy released by SNe decreases SF efficiency ( $c_*$ ) by means of:

- ▶ Destroying star forming clouds
- ▶ Generating supersonic turbulence
- ▶ Blow gas out of disc
- ▶ Number of SN produced in SSP of age  $t$

$$N_{SN}(t) = \int_{\max(m(t), m_{SN})}^{m_{max}} \frac{\Phi(m)}{m} dm$$

# AGN outflow

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SMBH may play an important role to outflow from galaxies that pollute IGM

- ▶ SNe not energetic enough to account for outflow
- ▶ Start simulation with BH seed that will accrete mass at a rate

$$\dot{M}_{BH} = \frac{4\pi\alpha G^2 M_{BH}^2 \rho}{(c_s^2 + v^2)^{3/2}}$$

- ▶ To compute this, a gas particle  $i$  around BH will be accreted with a probability

$$p_i = \frac{\omega_i \dot{M}_{BH} \Delta t}{\rho}$$

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- ▶ N-Body simulations are more than just gravitational evolution of systems
- ▶ **N-Body/SPH GADGET-2** proved a worthy sandbox to test models of galactic evolution
- ▶ Current steady growth in computer power → increase in spatial & temporal resolution leading to more accurate simulations

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